# Tree pattern queries: learning and teaching 

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## Trees and tree patterns (twigs)


(a) Tree $t_{0}$.
(b) Twig query $q_{0}$.

## Trees and tree patterns (twigs): embeddings


(c) Embeddings of $q_{0}$ in $t_{0}$.

## Unary tree patterns and decorated trees


(d) Unary path query $p_{0}$.

(e) Decorated trees $t_{1}$ and $t_{2}$.

## What is this talk about?

characterizing queries for a given $q$ provide a (polynomial) set of examples $C S_{q}$ such that for all $p$ it holds $C S_{q} \subseteq \mathcal{L}(p)$ iff $q \subseteq p$.

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Here, we focus on samples with positive examples only.


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Minimality vs. completeness?

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## Arbitrary twigs: problems

- sometimes queries are contained but no embedding exists, e.g., $r / a / / b$ and $r / * / *$
- containment is coNP-complete, subsumption (i.e., the existence of embeddings) is in PTIME
- moreover: exponential samples required


## Arbitrary twigs require exponential samples

Theorem
For any natural number $n$ there exists a twig query $q$ such that any set characterizing $q$ contains at least $2^{n}$ examples.

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Proof.
Construct a query $q$ and a set of twig queries $U$ such that:

1. for each $p \in U$ we have $q \nsubseteq p$;
2. no single positive example $t$ can witness the fact that any two distinct $p_{1}, p_{2} \in U$ are not equivalent to $q$;
3. $U$ contains $2^{n}$ queries.

## Arbitrary twigs require exponential samples


(f) Query $q$
(g) Query $p_{v}$ for $v=\left(k_{1}, \ldots, k_{n}\right)$.

## Anchored tree patterns: a good class

A twig query is anchored if:

1. A //-edge can be incident to a $\star$-node only if the node is a leaf.
2. A *-node may be a leaf only if it is either incident to a //-edge or it is the selecting node.

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## Anchored tree patterns: a good class

Theorem
For anchored twigs:
P1. subsumption $\equiv$ containment;
P2. a small characteristic sample always exists (two trees are enough!).

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## P2: Containment characterizing trees



## Lemma

Take any anchored query $q$ and construct $t_{1}^{q}$ as above. For any $p$ of height bounded by the height of $q$ and not using labels $a_{1}$ and $a_{2}$, $t_{1}^{q} \leqslant p$ implies $q \leqslant p$.

## P2: Containment characterizing trees



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Corollary
If both $t_{0}^{q}$ and $t_{1}^{q}$ satisfy $p$, then $q \subseteq p$.

## Learning for unary anchored path queries

Input: a sample $S$ of decorated trees
Output: a minimal unary anchored path query $p$ such that $S \subseteq \mathcal{L}(p)$

## Learning for unary anchored path queries

$w:=\min _{\leq_{\text {can }}}(\operatorname{SelPath}(S))$
let $w$ be of the form $r / a_{1} / \cdots / a_{n}$
$p:=r / / \star$
foreach subpath $u$ of $a_{1} / a_{2} / \cdots / a_{n-1}$
in the order of decreasing lengths do replace in $p$ any $/ /$-edge by $/ / u / /$ as long as $S \subseteq \mathcal{L}(p)$

## Learning for unary anchored path queries

let $p$ be of the form $r / / p_{0} / / b_{1}$
if $S \subseteq \mathcal{L}\left(p\left\{b_{1} \leftarrow a_{n}\right\}\right)$ then
$p:=p\left\{b_{1} \leftarrow a_{n}\right\}$

## Learning for unary anchored path queries

foreach descendant edge $\alpha$ in $p$ do find maximal $\ell$ s.t. $S \subseteq \mathcal{L}\left(p\left\{\alpha \leftarrow / /(\star /)^{\ell}\right\}\right)$
if $S \subseteq \mathcal{L}\left(p\left\{\alpha \leftarrow /(\star /)^{\ell}\right\}\right)$ then
$p:=p\left\{\alpha \leftarrow /(\star /)^{\ell}\right\}$
return $p$

## A sample and the constructed queries.



## Learning unary anchored path queries

Theorem
Our algorithm is sound and complete (i.e., it is sound and returns $q$ if the input is $S$ such that $\left.S \supseteq C S_{q}=\left\{t_{0}^{q}, t_{1}^{q}\right\}\right)$.

Proof.

- Assume some $p$ is returned for a given sample $S$.


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- Obviously, $S \subseteq \mathcal{L}(p)$.
- By case analysis: there is no $p^{\prime} \neq p$ such that $p^{\prime} \subseteq p$ and $S \subseteq \mathcal{L}\left(p^{\prime}\right)$.
- Since $C S_{q} \subseteq S \subseteq \mathcal{L}(p)$ then $q \subseteq p(\mathrm{P} 2)$. Hence, by the claim above, $p$ and $q$ are equivalent.


## Learning anchored queries

Our algorithm can be extended for

- boolean anchored path queries,
- conjunctions of anchored path queries,
- (path-subsumption-free) boolean twigs,
- (path-subsumption-free) unary twigs.

